# RHIC PROJECT

Brookhaven National Laboratory

Comments on the  $a_1$ ,  $b_1$  Correction System

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## COMMENTS ON THE $a_1,b_1$ CORRECTION SYSTEM

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## 1. a<sub>1</sub> Correction System

## $\nu$ -Shift Effect

Coupling introduces normal modes  $\nu_1, \nu_2$ .

## **Before Correction**

$$|\nu_1 - \nu_2|_{max} = 228 \times 10^{-3} \ \beta^* = 2$$

$$|\nu_1 - \nu_2|_{max} = 80 \times 10^{-3} \ \beta^* = 6$$

(G. Parzen, AD/RHIC-AP-81, 1989.)

## Global Correction System

 $a_1$  correctors in insertions at Q2 and Q5. Two families for each  $\beta^*$ . Q2 and Q5 for  $\beta^* = 6$ . Q2 for  $\beta^* = 2$ .

## After Correction (Residual $\Delta \nu$ )

 $\Delta \nu_{11}$  Stopband = 0 (Correct to make stopband = 0)

$$|\nu_1 - \nu_2|_{max} = 15 \times 10^{-3} \ \beta^* = 6$$

$$|\nu_1 - \nu_2|_{max} = 20 \times 10^{-3} \ \beta^* = 2$$

Empirical Correction (Correct to minimize  $|\nu_1 - \nu_2|$ )

$$|\nu_1 - \nu_2| = 7 \times 10^{-3} \ \beta^* = 6$$

$$|\nu_1 - \nu_2| = 12 \times 10^{-3} \ \beta^* = 2$$

Some additional  $a_1$  correctors needed to reduce  $|\nu_1 - \nu_2|$ .

Note the advantage of setting correctors empirically, rather than setting them to cancel the  $\nu_x = \nu_y$  stopband.

## Betatron Distortion due to Random a<sub>1</sub>

Indicated by large  $\beta_1, \beta_2 - \Delta \beta / \beta \simeq 60\%$  found.

Betatron distortion measured by coupling distribution factor, CDF

$$CDF = \frac{X_{max}(s)}{X_{max}(s)_{a_1=0}} \text{ for given } x_o, x'_o, y_o, y'_o$$

Usual assumption,  $CDF \simeq 1.4$  for  $\epsilon_{x,o} = \epsilon_{y,o}$ . Computer study gives

$$(CDF)_{max} \simeq 2$$

#### Consequences of Large CDF – Aperture Loss

a) Linear Aperture Loss

Calculations of aperture required, e.g. the extraction magnet, can be off by 40%.

b) Dynamic Aperture Loss  $(A_{SL} loss)$ 

At some QF,  $A_{SL}$  can be reduced by 40%. Average loss  $A_{SL}$  about 15%. (G. Parzen, AD/RHIC-AP-80, 1989.)

## Residual $|\nu_1 - \nu_2|$ and CDF Correction

<u>Proposal</u>: Separately excited  $a_1$  near each high  $\beta$  quad in the insertions. Twelve separately excited  $a_1$  near Q2.

This was also suggested by Correction System Review Committee.

This may correct both residual  $|\nu_1 - \nu_2|$  and the CDF.

 $a_1$  correctors near QD in arc may also be helpful but may not be necessary.

The above 3 effects, (1) the residual  $|\nu_1 - \nu_2|$ , (2) the high CDF and (3) the loss in  $A_{SL}$ , deserve careful consideration before giving up the  $a_1$  correctors in the arcs.

The  $a_1$  at Q2 are excited in two families to generate the cos and sin of the  $\nu_x + \nu_y$  harmonic. This gives a total of 4 knobs in the  $a_1$  correction system to control  $|\nu_1 - \nu_2|$  and the CDF.

Note that again the Q2 correctors are set empirically to reduce the CDF and the residual  $|\nu_1 - \nu_2|$ . They are not set to cancel out a  $|\nu_x + \nu_y|$  stopband.

Are two knobs sufficient to control the CDF and the residual  $|\nu_1 - \nu_2|$ ? Some judgment is needed as to what level of correction is sufficient.

#### 2. The $b_1$ Correction System

## $\Delta \beta / \beta$ Effects of Random $b_1$

$$\beta^* = 6 \quad (\Delta \beta/\beta)_{max} = 0.36$$

$$\beta^* = 2 \quad (\Delta \beta / \beta)_{max} = 0.90$$

 $(\Delta \beta/\beta)_{max} = 0.20$  comes from the arcs. Largest effect from Q1, Q2, Q3,  $\beta^* = 2$ . (G. Parzen, AD/RHIC-AP-71, 1988.)

Above is a large effect and needs correction. Most of this effect can be corrected using  $b_1$  corrections in the insertion quads.

<u>Proposal</u>: Use the  $b_1$  corrections in the insertion quads to also correct the 20% effect due the arc magnets, as well as the large effect due to Q1, Q2, Q3.

Note that the  $a_1$  effects and  $b_1$  effects are similar and of the same order. The  $b_1$  effects only appear smaller because of the availability of correction coils that are already there for other reasons. Both  $a_1$  and  $b_1$  produce a  $\nu$ -shift, a betatron distortion, and a loss in dynamic aperture.

Using the  $b_1$  coils in the insertions makes the  $b_1$  correction system and the  $a_1$  correction look similar.

<u>Proposal</u>: Use 4 knobs in the Q2, Q3 magnets to control the effects of the  $2\nu_x$  and  $2\nu_y$  resonances on  $\Delta\beta_x/\beta_x$  and  $\Delta\beta_y/\beta_y$ . This will produce a certain level of correction which may be sufficient. More knobs could be added, but would be difficult to use.

#### Why Correct $b_1$ ?

 $b_1$  effects may be larger than expected because of

- a) difficulty in correcting Q1, Q2, Q3
- b) closed orbit errors in sextupoles
- c) other various sources
- d) operating near the integer  $\nu$ -value.

#### 3. Dispersion Correction

$$\frac{\Delta X_p}{X_p} = 0.25 \text{ at QF}$$

$$\frac{\Delta Y_{p,max}}{Y_p} = 0.31 \text{ at QD}$$

Mostly from arc magnets. (G. Parzen, AD/RHIC-AP-71, 1988.)

## Reasons for Correcting $X_p, Y_p$

- 1) Effect on beam-beam interaction
- 2) To be able to operate near integer,  $\nu \simeq 29$ , where effect maybe about 3 times larger.

## Proposal:

- 1) Use  $a_1$  correctors at QD in arcs to correct  $Y_p$ . Possible  $a_1$  corrector near Q9 as a back-up correction.
- 2) Use  $b_1$  correctors at QF in arcs and  $b_1$  in insertion quads to correct  $X_p$ .

The only new correctors required by the proposals in this note are the  $a_1$  correctors at each Q2 in the insertions.